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A quantum phase transition driven by the electron lattice interaction gives high T_c superconductivity

A. Bianconi^{*}, S. Agrestini, G. Bianconi, D. Di Castro, N.L. Saini

Dipartimento di Fisica, *and Unita INFM ´ `* , *Universita di Roma* '*La Sapienza*', *P*. *le Aldo Moro* 2, ⁰⁰¹⁸⁵ *Roma*, *Italy*

Abstract

We identify for the first time the quantum phase transition (QPT) as a function of the electron lattice interaction for charge localization in stripes with local lattice distortions in cuprate perovskites at metallic densities. The electron lattice interaction $\lambda(\eta)$ is triggered at the localization limit by the strain η of the CuO₂ plane due to the chemical pressure generated by the mismatch between the copper oxide and the rocksalt layers. The strain of the CuO₂ plane has been directly measured by Cu K-edge EXAFS. The critical point for the charge localization in striped lattice domains coexisting with itinerant carriers is at η_c =0.04 ± 0.005 and δ_c =0.16 ± 0.03. We report a 2D plot T_c (δ,η) for the doped perovskites, where δ is the doping. The plot $T_c(\eta)$, for δ =constant, shows the highest T_c at the critical point η_c =0.04±0.01. The attractive pseudo Jahn–Teller (pJT) interaction and the particular critical charge and spin fluctuations driven by critical ordering of cooperative pJT local lattice distortions, forming a superlattice of quantum stripes tuned at a 'shape resonance' near this quantum critical point, provide a possible solution for two long standing mysteries: the phase diagram and the pairing mechanism in cuprate superconductors. \circ 2001 Elsevier Science B.V. All rights reserved.

Keywords: High T_c superconductors; Phase diagram; Pairing mechanism; Critical point; Stripes; Cooperative pseudo Jahn–Teller local lattice distortions; Incommensurate charge density wave; Intermediate coupling

The low temperature phase transitions in strongly corre- quasiparticle scattering rate and potentially to a breakdown lated electron systems remain only partially understood. of the Fermi liquid description in its simplest form $[2-4]$

generically continuous transition tuned by a parameter in the Hamiltonian. Near this transition quantum fluctuations conducting phase is in the regime of quantum fluctuations take the system between two distinct ground states. near a QPT from a metal to a spin ordered phase [11]. Examples of QPT include the metal-to-insulator transition In barium bismuthates $(Ba_{1}K, BiO_3)$ and in disordered alloys, the integer and fractional Quantum–
Hall transitions, magnetic transitions in heavy Fermion QPT to a charge ordered phase (CDW) due to valence Hall transitions, magnetic transitions in heavy Fermion QPT to a charge ordered phase (CDW) due to valence alloys, the superconducting-to-insulator transition in granu-
skipping $(Bi^{4+} - Bi^{3+} + Bi^{5+})$ [12]]. The supercond lar superconductors [1]. The unconventional normal state ing phase with a short coherence length in these materials can be described in terms of fluctuations of the local order has clear similarities with high T_c superconductors parameter. For example if the magnetic ordering tempera- (HTcS). ture in heavy Fermions is suppressed to absolute zero these The non Fermi liquid behavior of transport properties in fluctuations soften leading to strong enhancement of HTcS is an indication of the proximity to some unknown

An increasing number of systems are coming to light such The presence of non-conventional pairing mechanisms as heavy fermion and cuprate superconductors where the in superconductivity near a QPT is well established in Fermi liquid regime is suppressed due to their proximity to several exotic materials [5]. In several organic materials quantum phase transitions. $\qquad \qquad$ and heavy Fermions, CePd₂Si, [6], CeNi₂Ge, [7] and A quantum phase transition (QPT) is a zero temperature CeRh Si [8–10] the superconducting phase appears by 2 2

QPT. Several proposal have been presented for the pres-*Corresponding author. Tel.: +39-0649-914-405; fax: +39-0649-57- ence of a QCP at some critical value of the doping.

E-*mail address*: antonio.bianconi@roma1.infn.it (A. Bianconi). doping of the 2D AF Mott–Hubbard insulator, in fact a

^{697.} It has been proposed that the critical point is due to the

phenomenological model for the low energy spin dynamics the phase diagram of doped cuprate perovskites. Therefore in the normal state shows that these systems are close to a we have looked and found the QCP for the onset of the QPT [13,14]. However in this case the predicted maximum coexistence phase of polaronic stripes and itinerant carriers T_c is expected at the critical point for disappearing of AF in the intermediate coupling regime studying the physical order in the range $0.02 < \delta < 0.06$ [15] in disagreement with properties at constant doping as a funct the experiments. Other authors have considered a case of lattice coupling. QPT near a metal to insulating CDW phase transition in The pseudo Jahn–Teller electron–lattice interaction λ in the strong local electron–lattice interaction regime [16–18] cuprate families is driven by the strain η of the CuO₂ and in the weak coupling Hubbard–Holstein model plane. High T_c superconductors are heterogeneous m [19,20]. The first experimental evidence for a CDW with als made of alternated layers of metallic bcc CuO, layers its associated modulation of local lattice distortions (LLD) and insulating rocksalt fcc AO layers [50,51]. The bondwas found by joint X-ray diffraction and extended X-ray length mismatch across a block-layer interface is given by absorption fine structure (EXAFS) [21–40]. It was shown the Goldschmidt tolerance factor $t = [r(A-O)]/\sqrt{2}[r(Cu$ that the charge localization in the correlated 2D electron O)], where $[r(A-O)]$ and $[r(Cu-O)]$ are the respective gas is driven by cooperative pseudo Jahn–Teller (pJT) bond lengths in homogeneous isolated parent materials electron lattice interaction in the intermediate coupling $A-O$ and CuO, [52,53]. The hole doped cuprate perovregime (ICR). In the Bi2212 case the one-dimensional skite heterostructures are stable in the range $0 \ge t \ge 0.9$ that (1D) ordering of LLD form stripes that co-exist with corresponds to a mismatch $1 - t$ of $0 < 1 - t < 10$ %. The itinerant carriers. The resulting scenario of superconduct- $CuO₂$ sheets are under compression and (AO) layers under ing stripes in high T_c superconductors where 'the free tension in the hole doped cuprates showing high T_c .
charges move mainly in one direction, like the water The electron-lattice interaction of the pseudo JT ty running in the grooves of a corrugated iron foil', was first given by $\lambda = g(Q) f(\Delta_{IT}) h(\beta)$, where *Q* is the conformaintroduced in 1992 at Erice [21–23]. The 1D incommensu- tional parameter for the distortions of the CuO₄ square, rate CDW that co-exists with the superconducting phase is like the LTT-type tilting and its rhombic distortion; β is made of stripes of distorted lattice due to the freezing of the dimpling angle that measures the displacement of the pseudo Jahn–Teller Q_2 modes of the CuO₄ square lattice Cu ion from the plane of oxygens; and Δ_{JT} is the JT (LTT-like) [41] that are separated by domain walls of splitting that is modulated by the Cu–O (apical) bo (LTT-like) [41] that are separated by domain walls of undistorted lattice stripes (LTO-like). The size of the and/or β increase with the increasing strain η of the CuO₂ domain of cooperative local lattice distortions where the plane due to the mismatch. Therefore the domain of cooperative local lattice distortions where the plane due to the mismatch. Therefore the pseudo JT localized electrons are trapped was found to be 5 Å [34] in polaronic electron lattice interaction is a function agreement with an intermediate coupling regime. In small variations of η , in all cuprate perovskites 0.02 $\leq \eta$ Bi2212 with $T_c = 80$ K the charge ordering temperature 0.08, we can assume a proportionality between λ and η . was found to be 120 K. By changing the doping in Bi2212 We have directly measured the strain of the CuO, lattice the system remain always in the coexistence regime by measuring the Cu–O distances by in plane polarized (localized charges in the CDW and itinerant electrons) but Cu K-edge EXAFS. The 3D lattice structure has been is was never possible to find a critical density for the onset solved by X-ray diffraction. The anomalous X-ray diffracof CDW, i.e. a QCP for CDW. tion at the Cu K edge has been used to measure directly the

tronic topological transition [42], i.e. by tuning the chemi- charge and local lattice distortions has been detected by cal potential at a van Hove singularity was ruled out by the diffuse X-ray scattering using synchrotron radiation. The fact that the van Hove singularity is located at doping 0.25 strain $\eta = 2(1 - \langle Cu - O \rangle / d)$ for each sample has been [43]. $[43]$

pelling evidence for quantum critical fluctuations in high tance with no lattice mismatch $1 - t \sim \eta$. T_c superconductors [44,45]. Therefore the key problem to The superconducting critical temperature $T_c(\delta,\eta)$ of be solved to understand the pairing mechanism and phase many cuprate perovskites as a function of doping δ and the diagram in HTcS is the actual nature of the QPT and the CuO₂ strain η is plotted in Fig. 1. The cuprates

ous metallic phase of cuprates we are in a regime of occupy the upper region of Fig. 1 while those in the coexistence of localized and itinerant carriers [46,47]. The weaker electron–lattice interaction regime $0.02 \lt \eta \lt \eta_0$ standard plots $T_c(\delta)$ of La214 and Bi2212 do not cross the show quantum fluctuations of pJT LLD nea standard plots $T_C(\delta)$ of La214 and Bi2212 do not cross the quantum critical point. The electron lattice interaction strain $\eta_c = 0.04$. The maximum $T_c = 135$ K appears in the giving the CDW is well established by the isotope effect circle centered at the OCP at $\eta = \eta_c$. The high experiments [48] observed also for the stripe formation ductivity is suppressed around the black dots where the temperature [49]. It provides a second variable to describe commensurate polaron crystal (CPC) at δ = 0.125 appears

properties at constant doping as a function of the electron

plane. High T_c superconductors are heterogeneous materi-

The electron–lattice interaction of the pseudo JT type is

Quantum spin density wave fluctuations near an elec- diffraction due to only the Cu lattice. The 1D ordering of Recently some experiments have provided further com- \overline{EXAFS} where $d=1.97$ Å is the Cu–O equilibrium dis-

location of the quantum critical point (QCP). $(La_{1-x}Ba_xCuO_4, La_2CuO_{4+\delta}, La_{0.6}Nd_{0.4}La_{1-x}Sr_xCuO_4)$ All available experimental data show that in the anomal- with strain $0.08 > \eta > \eta_0$ larger than the strain $\eta_0 = 0.07$ circle centered at the QCP at $\eta = \eta_c$. The high T_c supercon-

of the CuO, plane. The elliptical blue area indicates the location of the rate crystal phase A at larger strain. The critical strain

appears with the minimum electron lattice interaction in expected. The superconducting phase is rapidly suppressed the families of $La_{1-x}Ba_xCuO_4$ and oxygen doped by the formation of the CPC that competes with the La₂CuO_{4+ δ} at the doping $\delta_0 = 1/8$ is identified by the superconducting order. The anomalous metallic phase in a

Fig. 2 shows the plot $T_c(\eta)$ at constant doping, $\delta = 0.16$, many experiments. i.e. for optimally doped samples, following the second Finally Fig. 4 shows a generic phase diagram in the vertical dashed line in Fig. 1. The plot $T_c(\eta)$ shows a intermediate coupling regime as a function of electron quantum critical point η_c ~0.04. In this regime the super-
lattice coupling and doping. The cuprates are at conducting phase extends well beyond the critical point for $\eta > \eta_c$ indicating that the particular superlattice of polaron stripes due to quantum LLD fluctuations can coexist and

polaron stripe formation in oxygen doped La214 and Bi2212 are shown temperature reaches a maximum at the critical mismatch $\eta_c = 0.04$. The by open squares at fixed doping $\delta = 0.16$. The superconducting critical critical temperature reaches a maximum at the critical strain $\eta_c \sim 0.04$. The stripes (phase A) and itinerant carriers (phase B) co-exist. The CPC (or critical point is the onset of the inhomogeneous phase, where pseudo JT the pure phase A) competes and suppresses the critical temperature for polaron stripes and conducting carriers co-exist. η > 0.07.

amplify the critical temperature in agreement with the well established 'shape resonance' amplification of the critical temperature for this particular ICDW [25,26,29].

In Fig. 3 we have reported the value of the critical temperature as a function of the lattice strain $T_c(\eta)$ at a fixed doping, $\delta = \delta_0$, (i.e. along the vertical dashed line passing across the black dot in Fig. 1). The superconducting phase appears below T_c in the green area. It is evident that the critical temperature reaches a maximum value near the critical value $\eta_c = 0.04$ that is the quantum critical point (QCP) shown in Fig. 1. The line separating the quantum fluctuation regime from the phase where local lattice distortions appear $(A+B$ and A) is the experimentally observed charge ordering temperature $T_{\rm co}$ for the oxygen doped La124 and Bi2212 systems at $\delta = 0.125$. This line separates the non Fermi liquid or quantum fluctuating Fig. 1. The experimental superconducting critical temperature T_c (δ , η) of
different superconducting cuprates as a function of strain η and doping δ ICDW and free carriers, and the pJT polaron commensu-QCP at the critical strain $\eta_c = 0.04$. $\eta_c = 0.04$ is the critical point for the onset of the polaron stripes which is associated with the critical point for spin ordering SDW. The quantum critical point at $\eta_c = 0.04$ in compounds with η > 0.07. This point P_0 where the CPC gives the highest superconducting transition temperature as black dot. $\qquad \qquad \text{quantum critical regime is expected at } \eta \sim \eta_c \text{ as shown by}$

lattice coupling and doping. The cuprates are at the critical point for the formation of local lattice distortions and the

Fig. 2. The superconducting critical temperature $T_c(\eta)$ (circles) as a Fig. 3. The superconducting critical temperature $T_c(\eta)$ (circles) as a function of the lattice strain η at $\delta_0 = 0.125$. The superconducting cri function of the lattice strain η at $\delta_0 = 0.125$. The superconducting critical critical point is the onset of the coexistence phase, where JT polaron

doped perovskites in the intermediate electron lattice coupling regime. Suppressed by the formation of the CPC. On the contrary Beyond the charge transfer Mott-Hubbard insulator there is a region of the high T_c superconductivity co-exists with the ICDW.

phase separation of a glassy phase (G) of an electron glass in the interval in the underdope the cuprates by changing the lattice strain that is shown in Fig. 1. $2\Delta/T_c$ ratio [41,42]. In the optimum doping regime δ ~

and itinerant carriers [52,53], i.e. in the intermediate superconducting phases where T_c depends from both electron–lattice coupling regime [54]. In this regime doping δ and lattice strain η of the CuO₂ layers. The between the strong coupling regime where all charges are anomalous normal phase of cuprate superconductors is trapped by local lattice distortions at metallic densities determined by an inhomogeneous phases with co-existing
(small polarons of radius between 5 and 2 Å), phase A and stripes of charges trapped in LLD (generalized pol the phase B of itinerant charges in the weak coupling and itinerant carriers that appears for an electron lattice regime and high densities there is regime of coexistence of interaction larger than a critical value λ_c . Lattice-charge two phases: the $A+B$ phase. It is well established that for stripes or polaron stripes appear in this critical fluctuation the single polaron (doping δ ~0) there is cross over from regime. The lattice mismatch η drives the electron lattice the localized to itinerant polaron. On the contrary at interaction to a QCP of a quantum phase transition. The metallic densities there is critical value of the electron–
lattice interaction indicated by the ellipse for the onset of superconducting critical temperature occurs at $\eta = n$. coexistence of localized and itinerant charge carriers [54]. These results show that the particular spin and charge Commensurate polaron crystals (CPC) appear in the phase critical fluctuations in the inhomogeneous phase of polaron A where all carriers are trapped in the distorted local stripes and itinerant carriers favor the superconducting domains, the black dots is the commensurate crystal pairing. appearing at $P_0(\delta_0, \eta_0)$ the lowest possible density δ_0 and electron lattice interaction $\eta_0 > \eta_c$. The region of high T_c superconductivity in Fig. 1 spans the small gray rectangle around the QCP at $\lambda = \lambda_c$ in Fig. 4. The rectangle around **Acknowledgements** the QCP indicate the region spanned by the electron lattice coupling $\lambda(\eta)$ in the cuprates by changing the strain of the This research has been supported by 'Istituto Nazionale CuO₂ plane that was plotted in Fig. 1 reaching λ_c at di Fisica della Materia' (INFM), by the 'Ministero decritical η_c . ll'Universita e della Ricerca Scientifica' (MURST) —

ductivity occurs at the critical point of the electron lattice interaction for the formation of local lattice distortions at metallic density. The electron–lattice interaction is driven at this critical point by the strain of the CuO₂ plane η controlled by the lattice mismatch between the metallic layers and the intercalated block layers.

The maximum T_c occurs at the critical point for the transition from a homogeneous metallic phase to an inhomogeneous metallic phase with coexisting polaron stripes and free carriers at η_c = 0.04. For 0.04 $\lt \eta$ < 0.07, by decreasing the temperature the materials exhibit a transition at $T_{\rm co}$ from the homogeneous to the inhomogeneous phase that can be defined as the temperature for the polaron stripe formation.

We can understand now the complex phenomenology of cuprates showing quite different superconducting and normal phases in the under-doped to over-doped regime. Fig. 4. The generic phase diagram of the electronic phases formed in For η > 0.07, at δ = 0.125, the high T_c superconductivity is

electron lattice interaction and high doping. The phase of commensurate in a low density inhomogeneous phase $(A+B)$ where the polaron crystals (CPC), region A, appear at strong λ and low doping. The number of free carriers is smaller than that of charges region of coexistence of itinerant carriers and carriers trapped in local trapped in LLD (generalized polarons in a intermediate lattice interactions (generalized polarons), phase $A + B$, shows a critical density 2D electr lattice interactions (generalized polarons), phase A+B, shows a critical
point, QCP, at $\lambda = \lambda_c$, indicated by a blue ellipse. The rectangle around the
QCP indicate the region spanned by the electron lattice coupling $\lambda(\$ 0.16, $r_s \sim 6-8$, the density of itinerant carries is larger than that of localized carriers.

onset of co-existence of localized charges trapped in LLD In conclusion, we have deduced a phase diagram for the superconducting critical temperature occurs at $\eta = \eta_c$.

In conclusion, we have shown that high T_c supercon- Programmi di Ricerca Scientifica di Rilevante Interesse

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